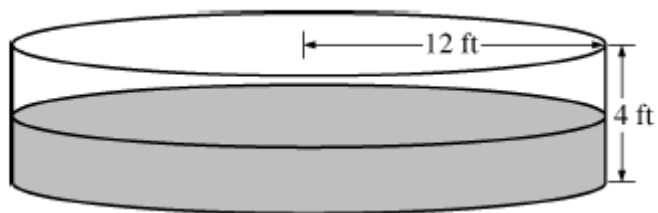


**“MR. CALCULUS” ANSWERS TO THE 2010 FORM B FREE RESPONSE QUESTIONS**

**AB/BC 3**

$t$	0	2	4	6	8	10	12
$P(t)$	0	46	53	57	60	62	63



At  $t = 0$ , the pool contains  $1000 \text{ ft}^3$  of water. Water pumped in at  $P(t) \frac{\text{ft}^3}{\text{hour}}$ .

Water leaking out at  $R(t) = 25e^{-0.05t} \frac{\text{ft}^3}{\text{hour}}$ .

(a) The midpoint Riemann sum is  $4P(2) + 4P(6) + 4P(10) = 4 \cdot (46 + 57 + 62) = \boxed{660 \text{ ft}^3}$

(b) The amount of water leaked out  $= \int_0^{12} R(t) dt \approx \boxed{224.594 \text{ ft}^3}$

(c) Volume = the initial amount plus the amount added less the amount leaked out.

So, the volume  $\approx 1000 + 660 - 225.594 = 1434.406 \approx \boxed{1434 \text{ ft}^3}$

(d) Let  $V(t)$  be the volume of water in the pool at time  $t$ . The volume of water in the pool is increasing at time  $t = 8$  at  $V'(8)$ .

$$V'(8) = P(8) - R(8) \approx 60 - 16.758 = \boxed{43.242 \frac{\text{ft}^3}{\text{hour}}}$$

$V = \pi r^2 h = 144\pi h$ , so  $V'(t) = 144\pi \frac{dh}{dt} \Rightarrow \frac{dh}{dt} = \frac{V'(t)}{144\pi}$ . Therefore,

$$\left. \frac{dh}{dt} \right|_{t=8} \approx \frac{43.242}{144\pi} \approx \boxed{0.096 \frac{\text{ft}}{\text{hour}}}$$