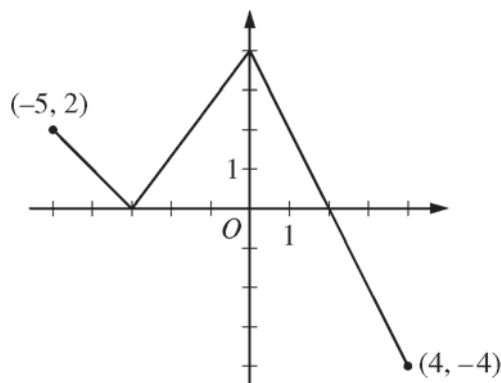


2014 AB/BC #3
(no calculator)



Graph of f

$g(x) = \int_{-3}^x f(t) dt \Rightarrow g'(x) = f(x)$ So this is also the graph of $g'(x)$.

(a) $g(3) = \int_{-3}^3 f(t) dt = \int_{-3}^2 f(t) dt + \int_2^3 f(t) dt = \boxed{\frac{1}{2}(5)(4) - \frac{1}{2}(1)(2)} = 9$

(The area of the 2nd triangle is subtracted since it is below the x -axis.)

(b)

g is increasing when g' or $f > 0 \Rightarrow -5 < x < 2$

g is concave down when g'' or $f' < 0 \Rightarrow g'$ or f is decreasing $\Rightarrow -5 < x < -3$ and $0 < x < 4$

Both occur when $\boxed{-5 < x < -3$ and $0 < x < 2$ }

(c)

$h(x) = \frac{g(x)}{5x} \Rightarrow h'(x) = \frac{5xg'(x) - 5g(x)}{25x^2}$ using the quotient rule

$h'(3) = \frac{5(3)g'(3) - 5g(3)}{25(9)} = \frac{15f(3) - 5(9)}{25(9)} = \boxed{\frac{15(-2) - 5(9)}{25(9)}} = -\frac{1}{3}$

(d)

$p(x) = f(x^2 - x) \Rightarrow p'(x) = (2x - 1)f'(x^2 - x)$

The slope of the tangent line to p at $x = -1$ is

$p'(-1) = (2(-1) - 1)f'((-1)^2 - (-1)) = (-3)f'(2) = \boxed{(-3)\left(\frac{-4 - 4}{4 - 0}\right)} = 6$